ACHARYA INSTITUTE OF TECHNOLOGY Bangalore - 560090

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Fourth Semester B.E. Degree Examination, Dec.2016/Jan.2017 Control Systems

Time: 3 hrs.

Max. Marks: 100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

PART - A

- 1 a. A mechanical system is shown in the Fig.Q.1(a).
 - i) Obtain the performance equations.
 - ii) Draw the electrical analog based on force-current analogy.

(08 Marks)

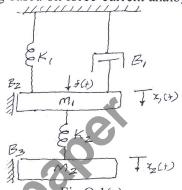


Fig.Q.1(a)

b. For the mechanical system shown in Fig.Q.1(b), draw the electrical network based on torque current analogy. Write the performance equations. (08 Marks)

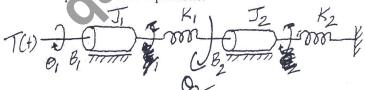


Fig.Q.1(b)

c. Write an explanatory note on gear trains.

(04 Marks)

- a. Define the term transfer function of a linear time invariant system. Derive the expression for the transfer function of a closed loop negative feedback system. (06 Marks)
 - b. For the block diagram shown in the Fig.Q.2(b), determine the overall transfer function using block diagram reduction rules. (06 Marks)

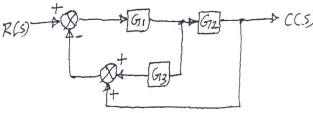


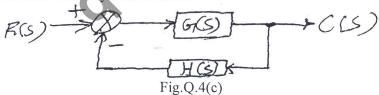
Fig.Q.2(b)

(08 Marks)

c. Consider the electrical circuit shown in Fig.Q.2(c). Find $\frac{V_0(s)}{V_i(s)}$ using Mason's gain formula.

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+ & R_1 & R_2 & \uparrow \\
V_2(t) & C_1 & C_2 & V_0(t) \\
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- a. Define the following terms with respect to an underdamped second order system:
 i) Peak time; ii) Settling time; iii) Steady state error.
 - b. A unity feedback system is characterized by an open loop transfer function $G(s) = \frac{K}{s(s+10)}$. Determine the gain K so that the system will have a damping ratio of 0.5. For this value of K, determine settling time, peak over shoot and time to peak overshoot for a unit step input. (08 Marks)
 - c. For a unity feedback system whose open loop transfer function is $G(s) = \frac{50}{(1+0.1s)(1+2s)}.$ Find the error constants K_p , K_v , K_a .
- a. State the Routh's stability criterion and mention its limitation.
 b. Consider the characteristic equation s⁶ + 2s⁵ + 8s⁴ + 12s³ + 20s² + 16s + 16 = 0. Using Routh's criterion, determine the stability of the system.
 - c. The closed loop system shown in Fig Q.4(c) has $G(s) = \frac{K(s+30)}{s(s+5)}$ and $H(s) = \frac{1}{(s+15)}$ Find the range of K for which system is stable. (08 Marks)



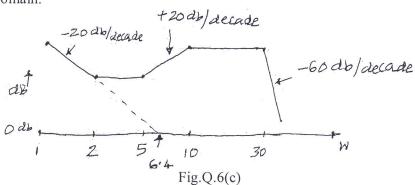
PART – B

5 a. Discuss the various rules for construction of root loci.

(08 Marks)

- b. A negative feedback control system is characterized by $G(s)H(s) = \frac{K}{s(s+1)(s+2)(s+3)}$. Sketch the root locus plot for values of K ranging from 0 to ∞ , Mark all the salient points on the root locus. (12 Marks)
- 6 a. Discuss the procedure to evaluate Gain margin and phase margin using Bode plots.
 (06 Marks)
 - b. Sketch the Bode plot for the transfer function $G(s) = \frac{Ks^2}{(1+0.2s)(1+0.02s)}$. Determine the system gain K for the gain cross over frequency to be 5 rad/sec. (08 Marks)

c. For the Bode magnitude asymptotic plot of Fig.Q.6(c), determine the transfer function in frequency domain. (06 Marks)



7 a. State the Nyquist stability criterion.

(06 Marks)

- b. Using the Nyquist stability criterion, investigate the stability of a closed loop system whose open loop transfer function is given by $G(s)H(s) = \frac{K}{(s+1)(s+2)}$. (14 Marks)
- 8 a. State the properties of state transition matrix.

(04 Marks)

b. Represent the electrical circuit shown in Fig.Q.8(b) by a state model.

(08 Marks)

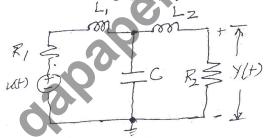
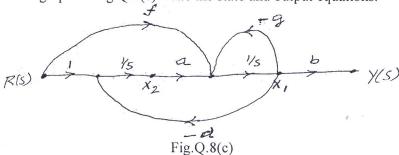


Fig.Q.8(b)

c. For the signal flow graph of Fig.Q.8(c) write the state and output equations:

(08 Marks)



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